The order in which commands are executed by a program is its flow of control. By default, statements are executed in the order in which they are given. However, a different execution order can be specified using what is known as a control structure. In this chapter we introduce two of Python’s most widely used control structures. The first, known as a for loop, is used to repeat a series of commands upon each element of a given sequence. The second control structure introduced in this chapter is a conditional statement (also known as an if statement). This allows a programmer to specify a group of commands that are only to be executed when a certain condition is true.

We will explain the basic syntax and semantics for these two control structures and show how they can be combined with each other to accomplish a variety of tasks. One common goal is to take an original list and produce a new list that is based upon a selection of elements from the first list that meet a certain criterion. This can be accomplished using a combination of the two control structures, yet Python supports a more concise syntax termed list comprehension.

This chapter serves to introduce these elementary control structures. We continue in Chapter 5 by introducing several more control structures. As a collective group, these provide great flexibility in designing code that is more elegant, robust, and maintainable.

### 4.1 For Loops

We often need to repeat a series of steps for each item of a sequence. Such a repetition is called iteration and expressed using a control structure known as a for loop. A for loop always begins with the syntax for identifier in sequence: followed by a block of code we call the body of the loop. The general schema of a for loop is diagrammed in Figure 4.1. As an example, we can print the name of each person from a guest list, one per line, with the following syntax.
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for identifier in sequence:
  body

FIGURE 4.1: General form of a for loop.

```python
for person in guests:
  print(person)
```

The identifier (i.e., `person`) is used like any other identifier in the language. Informally, we call this the *loop variable*; its name should suggest its meaning. The sequence (i.e., `guests`) can be any object that represents a sequence of elements, usually a list, string, or tuple. It can be specified with a literal, an identifier, or an expression that results in a sequence. At the end of that first line we use a colon (:) to designate the forthcoming body. The body itself (i.e., `print person`) specifies the command or commands that are to be executed for each iteration of the loop. This body is indented, although the precise amount of indentation is up to the programmer.

The semantics of a for loop is as follows. The identifier is assigned to the first item in the sequence and the body of the loop is executed. Then the identifier is reassigned to the next item of the sequence and again the loop body is executed. This iteration continues through the entire list. As a concrete example, consider the following loop, which might be used to generate name tags for a party:

```python
guests = ['Carol', 'Alice', 'Bob']
for person in guests:
  print('Hello my name is', person)
```

The changing value of identifier `person` during this iteration is diagrammed in Figure 4.2. When Python executes this loop, the actual flow of control is equivalent to the following series of statements:

```plaintext
person = 'Carol'
print('Hello my name is', person)
person = 'Alice'
print('Hello my name is', person)
person = 'Bob'
print('Hello my name is', person)
```

Of course, the advantage of the for loop syntax is that it allows us to express this repetition succinctly and for a general sequence of elements, rather than specifically for 'Carol', 'Alice', and 'Bob'.
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FIGURE 4.2: The assignment of person during three iterations of a for loop.

⚠️ A WORD OF WARNING

Although a for loop can technically iterate upon an empty sequence, the body of the loop is never executed; there are no elements.
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As a more interesting application, suppose that a bank keeps a chronological log of all transactions for an individual’s account. We model this as a list of numbers, with a positive entry representing a deposit into the account and a negative entry, a withdrawal. With this representation, the bank can perform many common tasks. For example, the overall balance for the account is simply the sum of all transactions (keeping in mind that “adding” a withdrawal decreases the balance). This sum can be computed as follows:

```python
balance = 0  # initial balance
for entry in transactions:
    balance = balance + entry
print 'Your balance is', balance
```

Figure 4.3 shows the progression of this code on a simple example. The top drawing represents our state immediately before the loop is reached. Notice that balance is explicitly initialized to zero prior to the loop. The three remaining diagrams show the state at the end of each of the three passes of the loop. By the final configuration, we have calculated the true balance. The `print` statement is not part of the body of the loop because it is not indented. So that command is only executed once, after the loop is complete.

We use this example as a demonstration, but we can simplify our code by taking better advantage of Python. First, Python supports an operator `+=` that adds a value to a running total. So the body of our loop could be expressed as

```python
balance += entry
```

rather than as `balance = balance + entry`. Corresponding shorthands exist for other arithmetic operators (e.g., `-=` , `*=` , `/=` , `//=` , `%=`). More importantly, computing the sum of a list of numbers is such a common task, there exists a built-in function `sum(transactions)`, which returns the sum (presumably by performing just such a loop internally).

As our next example, let `['milk', 'cheese', 'bread', 'cereal']` represent the contents of list `groceries`. Our goal is to output a numbered shopping list, as

1. milk
2. cheese
3. bread
4. cereal

We can generate this output using the following code fragment:

```python
count = 1
for item in groceries:
    print str(count) + ' . ' + item
    count += 1
```

Unlike our earlier examples, the body of this loop consists of multiple statements. Python relies upon the indentation pattern for designating the loop body. Since the command `count += 1` is indented accordingly, it is part of the body.
FIGURE 4.3: The changing state of variables as we compute the sum of a list. The top picture shows the state just before the loop. Subsequent pictures show the state at the end of each iteration.
Specifying loops from the interpreter prompt

We typically execute code that has been saved in a file. Yet it is possible to designate a loop as part of an interactive session with the Python interpreter. Try the following:

```python
>>> guests = ['Carol', 'Alice', 'Bob']
>>> for person in guests:
... ...
```

After entering the second line, Python does not immediately present its usual `>>>` prompt. The interpreter recognizes the beginning of a control structure that is not yet complete. Instead, it presents the `...` prompt (or if using IDLE, that next line is automatically indented to await our command). If we continue by specifying the indented command `print person` we find the following response:

```python
>>> guests = ['Carol', 'Alice', 'Bob']
>>> for person in guests:
...   print person
...
```

The interpreter still does not execute the for loop. Since a loop body might have more than one statement, the interpreter cannot yet be sure whether the body is complete. For this reason, the end of a body is designated by a separate empty line when working interactively. Only then does the loop execute, as seen in the following:

```python
>>> guests = ['Carol', 'Alice', 'Bob']
>>> for person in guests:
...   print person
... Carol
... Alice
... Bob
>>> 
```

Notice that a new `>>>` prompt is presented at the very end, once the loop has executed.

A WORD OF WARNING

Although a mix of tabs and spaces may appear to be equivalent indentation to you, they are not considered identical to the Python interpreter. You must be consistent in your usage or avoid tabs altogether. Some editors will automatically convert tabs to spaces for this reason.
4.1.1 Index-Based Loops

The `range` function, introduced in Section 2.2.4, generates a list of designated integers. These ranges are quite convenient for iteration in the context of a `for` loop. For example, the following code produces a countdown for a rocket launch:

```python
for count in range(10, 0, -1):
    print(count)
print('Blastoff!')
```

Ranges can often serve as a sequence of valid indices for another list. For example, let’s go back and look at the goal of producing a numbered shopping list. On page 128 we accomplished this by using a traditional loop over the elements of the list and keeping a separate counter for numbering. Another approach is to base our loop on the list `range(len(groceries))`. This produces a list of integers ranging from 0 up to but not including `len(groceries)`. So when the length of our grocery list is 4, the result is a list `[0, 1, 2, 3]`. By iterating over that list of numbers, we can use each index to generate the appropriate label as well as to access the corresponding list entry. Although we want our displayed labels numbered starting with one, we must recognize that indices of a list start at zero. Our code is as follows:

```python
for position in range(len(groceries)):
    label = str(1 + position) + '. '  # label is one more than index itself
    print(label + groceries[position])
```

To better understand this code, we examine its behavior on a grocery list with contents `['milk', 'cheese', 'bread', 'cereal']`. The loop iterates over positions in the range `[0, 1, 2, 3]`. The key expressions for each iteration are shown in the following table:

<table>
<thead>
<tr>
<th>position</th>
<th>label</th>
<th>groceries[position]</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>'1. '</td>
<td>'milk'</td>
</tr>
<tr>
<td>1</td>
<td>'2. '</td>
<td>'cheese'</td>
</tr>
<tr>
<td>2</td>
<td>'3. '</td>
<td>'bread'</td>
</tr>
<tr>
<td>3</td>
<td>'4. '</td>
<td>'cereal'</td>
</tr>
</tbody>
</table>

This technique, called an index-based loop, is especially helpful for tasks that require explicit knowledge of the position of an element within the list. As a motivating example, consider the goal of converting each name of a guest list to lowercase. A (flawed) first attempt to accomplish this might be written as

```python
for person in guests:
    person = person.lower()
```
Unfortunately, this code does not work as intended. Before suggesting a fix, let’s make sure that we understand the shortcomings of the attempt. The issue working against us is that we have a list of strings, yet strings are immutable objects. The command `person = person.lower()` generates a new string that is a lowercase version of the original, and then reassigns identifier `person` to that result. This has no effect on the original element in the list. Figure 4.4 diagrams the first iteration of this loop. When the second iteration of the loop begins, the identifier `person` will be reassigned to the second element of the list, but the execution of the body produces another auxiliary string.

Going back to our goal, since we cannot mutate the original elements of the list we must mutate the list itself. We can replace one entry of a list with a new value using a syntax such as `guests[i] = newValue`, but this requires knowledge of the element’s index within the list. We use an index-based loop as a solution.

```python
for i in range(len(guests)):
    guests[i] = guests[i].lower()  
```
As before, the right-hand side of the expression `guests[i] = guests[i].lower()` evaluates to a new lowercase string. But this time, the assignment statement has the effect of altering the list composition. With practice, the choice between traditional loops and index-based loops will become more clear. The index-based form is generally used when the behavior of the loop body depends upon the location of an item within the list; otherwise, the traditional form is preferred.

### 4.1.2 Nested Loops

We have already seen examples where the body of the loop includes several statements. In fact, the body can even include another loop. The technique of using one control structure within the body of another is called nesting. As a first example, consider the following code fragment:

```python
for chapter in ('1', '2'):
    print 'Chapter ' + chapter
    for section in ('a', 'b', 'c'):
        print '  Section ' + chapter + section
print 'Appendix'
```

To understand the behavior of this code, we view the nesting hierarchically. Line 1 defines a loop, which we will refer to as the outer loop. The body of this loop consists of lines 2–4. We recognize this because an indentation level is established at line 2, and the code remains indented at least this much until line 5. Since line 5 is back to the original level of indentation, it is not part of the outer loop body. In essence, the indentation allows us to abstract the high-level structure of the code as follows.

---

**A WORD OF WARNING**

We gave an example of a for loop that iterates through an underlying list while mutating that list. However, the mutation was a one-for-one replacement of an element of that list and so the overall structure of the list remained intact.

The behavior of a for loop is unpredictable if the underlying list is mutated in a way that alters its overall structure. In the following example, we remove and reinsert elements as the loop is executing. Can you guess how it will behave?

```python
original = ['A', 'B', 'C', 'D', 'E', 'F']
for entry in original:
    print entry
    original.remove(entry)
    original.append(entry)
```
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```python
for chapter in ('1', '2'):
    # the loop body
    # will be repeated
    # for each chapter
    print 'Appendix'

print 'Chapter ' + chapter
for section in ('a', 'b', 'c'):
    print ' Section ' + chapter + section
```

Although we are blurring over the details of the loop body, we can already see that the body will be executed with `chapter` set to '1', then re-executed with `chapter` set to '2', and finally the word 'Appendix' printed at the conclusion of the loop. Now, let's focus narrowly on the body.

```python
print 'Chapter ' + chapter
for section in ('a', 'b', 'c'):
    print ' Section ' + chapter + section
```

In isolation, this block of code is straightforward. Assuming that the identifier `chapter` is well defined, line 2 prints out a single statement, and lines 3–4 comprise a loop. For example, if someone told us that `chapter` was set to '1', then it would be easy to see that this block of code produces the following output:

```
Chapter 1
    Section 1a
    Section 1b
    Section 1c
```

We could similarly determine the output that would be produced if `chapter` were set to '2'. Going back to the original version, we can put all the pieces together to predict the following output:

```
Chapter 1
    Section 1a
    Section 1b
    Section 1c
Chapter 2
    Section 2a
    Section 2b
    Section 2c
Appendix
```

The use of nested control structures can lead to many interesting behaviors. We demonstrate one such example as part of the case study in Section 4.3 in the context of drawing graphics. We will see many more examples of nested control structures as we implement more complex behaviors.
4.2 Case Study: DNA to RNA Transcription

A strand of DNA is composed of a long sequence of molecules called nucleotides or bases. Only four distinct bases are used: adenine, cytosine, guanine, and thymine, which are respectively abbreviated as A, C, G, and T. An organism uses DNA as a model when constructing a complementary structure called RNA. This process of creating RNA from DNA is known as transcription. The RNA is then used to create proteins.

RNA also consists of four nucleotides, three of them being A, C, and G, and a fourth one uracil, which is abbreviated as U. Transcription creates an RNA sequence by matching a complementary base to each original base in the DNA, using the following substitutions:

<table>
<thead>
<tr>
<th>DNA</th>
<th>RNA</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>U</td>
</tr>
<tr>
<td>C</td>
<td>G</td>
</tr>
<tr>
<td>G</td>
<td>C</td>
</tr>
<tr>
<td>T</td>
<td>A</td>
</tr>
</tbody>
</table>

In this case study, we develop a program that asks the user to enter a DNA sequence and returns the transcribed RNA. An example session will look like

Enter a DNA sequence: AGGCTACGT
Transcribed into RNA: UCCGAUGCA

Our complete program is in Figure 4.5. The strings established in lines 1 and 2 encode the substitution rules for transcription. Those letters are intentionally ordered to give the proper mapping from DNA to RNA. Since the dna string entered by the user is itself a sequence, we use the for loop starting at line 6 to iterate through each individual DNA character. Line 7 finds the index of the DNA character within the dnaCodes. That index determines a corresponding RNA base from rnaCodes at line 8, which is then added to an auxiliary list rnaList at line 9. The overall RNA string is compiled at line 10, as the join of rnaList.

```python
dnaCodes = 'ACGT'
rnaCodes = 'UGCA'

dna = raw_input('Enter a DNA sequence: ')
rnaList = []
for base in dna:
    whichPair = dnaCodes.index(base)  # index into dnaCodes
    rnaLetter = rnaCodes[whichPair]   # corresponding index into rnaCodes
    rnaList.append(rnaLetter)

rna = '' .join(rnaList)  # join on empty string
print 'Transcribed into RNA: ', rna
```

FIGURE 4.5: Transcribing DNA to RNA.
4.3 Case Study: Drawing a Pyramid

In this case study, we develop two different programs for drawing a picture of a pyramid. In the first version a level is drawn as a single rectangle, while in the second a level is composed of individual squares. An example of each style is shown in Figure 4.6.

We begin by examining the first style. Our goal is not simply to draw the exact picture of Figure 4.6(a), but to develop a more general program that allows us to easily adjust the number of levels and the relative size of the drawing. To aid in the development of our code, we begin by assigning meaningful identifiers to two key measures: the number of levels and the desired height of each individual level.

```
numLevels = 8  # number of levels
unitSize = 12  # the height of one level
```

The unitSize serves as the height of each level and indirectly as a factor in determining the width of a level. For example, when setting the overall width and height of the canvas, we do not use numeric literals, but instead the expression unitSize * (numLevels + 1). This provides enough space for all of the levels, together with a small amount of margin around the pyramid.

```
screenSize = unitSize * (numLevels + 1)
paper = Canvas(screenSize, screenSize)
```

By writing the rest of our program to depend upon these named variables rather than the actual numbers, it becomes easy to later change the proportions of our pyramid.

Next, we must construct the levels of the pyramid. The biggest challenge is to get the details of the geometry correct. Although the levels are not identical to each other, there is clearly a repetitive pattern. We build the pyramid level by level, using a for loop that begins as follows.
FIGURE 4.7: Geometric sketch for a 4-level pyramid. The dotted lines mark units in the coordinate system. The solid rectangles represent the levels of the pyramid, with each dot highlighting the desired center point for a level.

```
for level in range(numLevels):
```

With this convention, level will iterate over values [0, 1, 2, 3, 4, 5, 6, 7] for the case of eight levels. For convenience, we build the pyramid starting at the topmost level. Therefore level 0 is at the top, level 1 is the one under that, and so on (yes, we realize that in real life, it helps to build the bottom of the pyramid first!). In designing the rest of the code, we must determine the inherent geometric pattern. Each rectangle in our figure must be defined with a specific width, height, and center point. Sometimes it helps to sketch a small example by hand to determine the pattern. Figure 4.7 provides such a sketch for a 4-level pyramid. From this sketch, we can develop the following table of values, remembering that the origin of the screen is at the top left corner:

<table>
<thead>
<tr>
<th>level</th>
<th>width</th>
<th>height</th>
<th>centerX</th>
<th>centerY</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1</td>
<td>1</td>
<td>2.5</td>
<td>1</td>
</tr>
<tr>
<td>1</td>
<td>2</td>
<td>1</td>
<td>2.5</td>
<td>2</td>
</tr>
<tr>
<td>2</td>
<td>3</td>
<td>1</td>
<td>2.5</td>
<td>3</td>
</tr>
<tr>
<td>3</td>
<td>4</td>
<td>1</td>
<td>2.5</td>
<td>4</td>
</tr>
</tbody>
</table>

We see both similarities and differences among the levels. Each level has the same height, namely the unitSize, yet the width varies. Examining the table, we see that the width of a level is precisely one more than the level number (as level 0 has width 1, level 1 has width 2, and so on). So within each iteration of the loop, we compute the proper width and construct a new rectangle as follows:

```
width = (level + 1) * unitSize  # width varies by level
block = Rectangle(width, unitSize)  # height is always unitSize
```

Placing each rectangle requires an understanding of the pattern from our sample geometry. The center x-coordinate is the same for each level, in fact it is precisely half of the screenSize. Since this value is the same for all levels, we can compute it once before the loop begins, rather than recomputing within the body of the loop. On the other hand,
from cs1graphics import *

numLevels = 8 # number of levels
unitSize = 12 # the height of one level
screenSize = unitSize * (numLevels + 1)
paper = Canvas(screenSize, screenSize)
centerX = screenSize / 2.0 # same for all levels

# create levels from top to bottom
for level in range(numLevels):
    width = (level + 1) * unitSize # width varies by level
    block = Rectangle(width, unitSize)
    centerY = (level + 1) * unitSize # height is always unitSize
    block.move(centerX, centerY)
    block.setFillColor('gray')
paper.add(block)

FIGURE 4.8: Code for drawing a pyramid made of rectangles.

the y-coordinate varies between levels so we recompute it within the body of the loop. Fortunately, we see a familiar pattern with level 0 having a value of 1, level 1 a value of 2, and so on. Our complete code is given in Figure 4.8. Notice that the central x-coordinate is computed only once, prior to the loop at line 7. The individual y-coordinates are computed within the body of the loop at line 13, and then assigned to the rectangle at line 14. Line 16 adds each block to the canvas.

In conclusion, we wish to emphasize the advantage of relying upon the named variables numLevels and unitSize. By simply altering lines 3 and 4, we can reconfigure the pyramid’s geometry. No other lines of code need to be changed. As a simple exercise, you could prompt the user for those key parameters. Another amusing modification is to make an animation of the process. By importing the time module and then inserting the command sleep(1.0) within the body of the loop, the visual construction of the pyramid will proceed level by level.

Pyramid made of squares

We next turn our attention to the second goal, a version of the pyramid made entirely from squares rather than rectangles, as shown in Figure 4.6(b). The general idea is quite similar; in fact the first ten lines of the code are identical. We create a screen of the appropriate size, and then begin a loop to create the pyramid, one level at a time. The difference in our two versions involves the body of the loop, since that determines how each level of the pyramid is built. In our first version, this body creates a single rectangle. In our next version, we use a nested loop to create and position a series of squares that comprise the level. Again, it helps to graph a small example. We find the general pattern is that level $k$ is comprised of $(k + 1)$ unit squares. All of the squares on a given level are centered with the same y-coordinate. In fact, this is the same coordinate that we used when centering
the rectangle in our first version. In this case, we compute it at line 12, prior to the inner loop. What differs among those squares is the x-coordinate. We approach the design by first considering where the leftmost square should be centered. By considering the width of the level, we determine the following equation:

\[
\text{leftmostX} = \text{centerX} - \text{unitSize} \times \text{level} / 2.0
\]

As a check, notice that the leftmost square of level 0 will be placed precisely at the center of the diagram. The leftmost square of level 1 will be one-half a unit to the left of center, and so on. With that knowledge, we place all of the squares of the level using an inner loop that begins as follows:

```python
for blockCount in range(level + 1):
    block = Square(unitSize)
    block.move(leftmostX + unitSize * blockCount, centerY)
```

Based on the selected range, we view the blocks of our level numbered from left to right, so that the leftmost is block 0, the one after that block 1, and so on. The x-coordinate of each block is set based upon an offset from the leftmost x-coordinate. So block 0 is the leftmost, block 1 is centered one full unit to the right of that, and so on. The complete second version of our code is given in Figure 4.9.

```
from cs1graphics import *

numLevels = 8          # number of levels
unitSize = 12          # the height of one level
screenSize = unitSize * (numLevels + 1)
paper = Canvas(screenSize, screenSize)
centerX = screenSize / 2.0  # same for all levels

# create levels from top to bottom
for level in range(numLevels):
    centerY = (level + 1) * unitSize
    leftmostX = centerX - unitSize * level / 2.0
    for blockCount in range(level + 1):
        block = Square(unitSize)
        block.move(leftmostX + unitSize * blockCount, centerY)
        block.setFillColor('gray')
paper.add(block)
```

**FIGURE 4.9:** Code for drawing a pyramid made of squares.
4.4 Conditional Statements

Our next control structure is known as a conditional statement or, more commonly, an if statement. It allows us to specify one or more instructions that are only to be executed when a certain condition is true. This is an extremely valuable tool as it allows execution to vary depending upon values that are not known until the program is running, such as input received from a user, data read from a file, or other forms of information that cannot be determined at the time the software is being written. A very simple example using a conditional statement is the following:

```python
dinner = raw_input('What would you like for dinner? ')
if dinner == 'pizza':
    print 'Great!'
    print 'I love pepperoni and black olives.'
```

The first line gets input from the user. The conditional construct is on lines 2–4. It begins with the keyword if followed by a boolean expression which we call the condition. That condition is followed by a colon and then an indented body. This format is shown in Figure 4.10. The semantics of a conditional statement is quite natural. If the condition evaluates to True, the body is executed; if the condition evaluates to False, the body is bypassed. This flow of control of an if statement is portrayed graphically in Figure 4.11.

The condition

The condition (e.g., dinner == 'pizza') can be an arbitrary boolean expression, as introduced in Section 2.8.2. This may be a single variable of type bool, or a more complex expression that evaluates to a boolean. The challenge for a programmer is crafting a condition that captures the desired semantics. Consider the following rule:

```python
if len(groceries) > 15 or 'milk' in groceries:
    print 'Go to the grocery store'
```

With this condition, we go to the store whenever we need lots of things or whenever we need more milk (even if few other things). This is very different from the following:

```python
if len(groceries) > 15 and 'milk' in groceries:
    print 'Go to the grocery store'
```

In this case, we only go to the store when we need lots of things including milk.
The body

Following the statement of the condition is the body of the conditional. As is the case with the for loop, the first statement of the body establishes a level of indentation for the rest of the body. The body can be as simple as one line, or more generally a larger block of code.

We can even nest one conditional within the body of another. Consider the scenario of a person approaching the site of a party, with someone guarding the door. The response of the guard may depend on whether the party has started and whether the person is on the guest list. Here is a reasonable behavior for the guard:

```python
if partyStarted:
    if person in guests:
        print 'Welcome'
```

First, the guard checks to see if the party has started. If the party has started, then the guard must test the second condition to see whether this individual is invited. It is only in the case where both conditions succeed that the actual `print` statement is executed. Notice that when the party has not started, the guard does not even bother checking the guest list. The result of such a check is irrelevant and performing the test could be time consuming for a large party. Interestingly, this nested logic is identical to the evaluation of a single compound conditional.

```python
if partyStarted and person in guests:
    print 'Welcome'
```

The outcome is clearly the same; the `print` statement executes only when both conditions are true. Yet the evaluation mechanism is similar as well. Python uses a technique known as short circuiting, where a partial evaluation of a boolean expression suffices as soon as
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Excerpt from “Object-Oriented Programming in Python” by Michael H. Goldwasser and David Letscher

Although we suggested that a condition must be a boolean expression, Python actually allows many other data types to be used as a condition. For example, when a sequence serves as the condition, the body of the statement is executed if that sequence is nonempty. Thus we may write

```python
if waitlist:
```

as a compact shorthand for the actual boolean expression

```python
if len(waitlist) > 0:
```

The same style can be used to differentiate between empty strings and nonempty strings. For example, the following code demonstrates a common technique for prompting the user for information while providing a default value when the user presses the enter key without typing any other characters.

```python
dinner = raw_input('What would you like for dinner? ')
if not dinner:
    # empty string entered by user
dinner = 'pizza'
```

Based on the condition `not dinner`, the body will be executed only when `dinner` is an empty string (i.e., when it does not have length greater than zero).

The use of a nonboolean object as a condition allows experienced programmers to make code more concise. However, there are pitfalls for a beginner who accidentally uses a nonboolean object. Consider the following code, which is syntactically legal but tragically flawed:

```python
response = raw_input('Shall we play a game? ')
if response == 'y' or 'yes':
    # play the game
```

The condition is treated as if it were parenthesized as follows:

```python
if (response == 'y') or ('yes'):
```

Since the right-hand operand of the `or` is a nonempty string, the overall condition will be treated as `True`, regardless of the actual `response` value. Of course, this can be a very nasty bug to uncover, as the condition will seem to be satisfied even when the user types 'Definitely not'.

By the way, one way to express the intended logic is with the condition `response == 'y' or response == 'yes'`. An even more concise form uses a containment check on a tuple, with the condition `response in ('y', 'yes')`.

---

For the Guru

Although we suggested that a condition must be a boolean expression, Python actually allows many other data types to be used as a condition. For example, when a sequence serves as the condition, the body of the statement is executed if that sequence is nonempty. Thus we may write

```python
if waitlist:
```

as a compact shorthand for the actual boolean expression

```python
if len(waitlist) > 0:
```

The same style can be used to differentiate between empty strings and nonempty strings. For example, the following code demonstrates a common technique for prompting the user for information while providing a default value when the user presses the enter key without typing any other characters.

```python
dinner = raw_input('What would you like for dinner? ')
if not dinner:
    # empty string entered by user
dinner = 'pizza'
```

Based on the condition `not dinner`, the body will be executed only when `dinner` is an empty string (i.e., when it does not have length greater than zero).

The use of a nonboolean object as a condition allows experienced programmers to make code more concise. However, there are pitfalls for a beginner who accidentally uses a nonboolean object. Consider the following code, which is syntactically legal but tragically flawed:

```python
response = raw_input('Shall we play a game? ')
if response == 'y' or 'yes':
    # play the game
```

The condition is treated as if it were parenthesized as follows:

```python
if (response == 'y') or ('yes'):
```

Since the right-hand operand of the `or` is a nonempty string, the overall condition will be treated as `True`, regardless of the actual `response` value. Of course, this can be a very nasty bug to uncover, as the condition will seem to be satisfied even when the user types 'Definitely not'.

By the way, one way to express the intended logic is with the condition `response == 'y' or response == 'yes'`. An even more concise form uses a containment check on a tuple, with the condition `response in ('y', 'yes')`.
the outcome can be properly determined. When the left-hand side of the \texttt{and} operator fails (in this case \texttt{partyStarted}), it reports \texttt{False} as the overall result without bothering to check the second condition. A similar optimization is used when the first clause of an \texttt{or} operator is \texttt{True}.

As another illustration of nested control structures, we return to the example of a list of bank account transactions. We used a for loop to calculate the overall sum of the transactions, and thus the final balance. Yet for a series of transactions to be legitimate, the intermediate balance should remain nonnegative throughout the process. Here is a variant of our original code that uses a conditional to check for such inconsistencies.

\begin{verbatim}
balance = 0
for entry in transactions:
    balance += entry
    if balance < 0:
        print 'Overdraft warning'
\end{verbatim}

\subsection*{4.4.1 if-else Syntax}

In its simplest form, a conditional is used to specify instructions that are executed when a given expression is \texttt{True}. An alternate set of steps can be expressed as an \texttt{else} clause, to be performed when the condition is \texttt{False}. Consider the following:

\begin{verbatim}
dinner = raw_input('What would you like for dinner? ')
if dinner == 'pizza':
    print 'Great!'
    print 'I love pepperoni and black olives.'
else:
    print 'How about pizza?'\end{verbatim}

The general syntax of an \texttt{if-else} statement is given in Figure 4.12. The associated semantics are shown by the flowchart in Figure 4.13. If the condition is \texttt{True}, the first body will be executed; otherwise the second body will be executed. As a more elaborate example, the following code computes separate totals for the deposits and withdrawals of a list of transactions (rather than the overall sum).

\begin{verbatim}
if condition :
    body1
else:
    body2
\end{verbatim}

\textbf{FIGURE 4.12:} Schema of an if-else statement.
Chapter 4   Elementary Control Structures

For each individual entry, we add it to one side of the ledger or the other based upon whether it is a positive value.

4.4.2 if-elif Syntax

Next, we revisit our rule for buying groceries, as originally given on page 140. By that logic, we make a trip to the grocery store whenever we need lots of things or whenever we run out of milk. With nested conditionals, we can define the following more intricate rule:

```
if len(groceries) > 15:
    print 'Go to the grocery store'
else:
    if 'milk' in groceries:
        print 'Go to the convenience store'
```

When we need lots of things we will make a trip to the grocery store, but we do not bother going to the grocery store when our list is short. Instead, we consider making a quick trip to the convenience store based upon a second condition, namely that we need milk. A flowchart for this logic is given in Figure 4.14. There are three possible paths through this chart: we might go to the grocery store, we might go to the convenience store, or we might...
Section 4.4 Conditional Statements

len(groceries) > 15  True

Grocery Store

len(groceries) > 15  False

'\texttt{milk}' in groceries  True

Convenience Store

'\texttt{milk}' in groceries  False

(\texttt{nothing})

FIGURE 4.14: Flowchart for an \texttt{if-elif} statement.

Placing a second conditional within the body of an else clause is so common, Python supports a convenient shorthand using the keyword \texttt{elif} (short for “else if”), followed by a secondary boolean expression. Thus the above example could be rewritten as

```
if len(groceries) > 15:
    print 'Go to the grocery store'
elif 'milk' in groceries:
    print 'Go to the convenience store'
```

The distinction may seem slight in this first example, but an advantage is that we avoid increasing the level of indentation when there are additional conditions.
More generally, we can chain together multiple `elif` clauses and optionally a final `else` clause. To demonstrate this use, we consider the following biological application. Recall from the case study of Section 4.2 that DNA strands are often represented as long character strings over the bases A, C, G, and T. A simple computational task is to count the number of occurrences of each individual base within a string `dna`. We can accomplish this using the following implementation:

```python
numA = numC = numG = numT = 0
for base in dna:
    if base == 'A':
        numA += 1
    elif base == 'C':
        numC += 1
    elif base == 'G':
        numG += 1
    else:  # presumably a T
        numT += 1
```

The first line initializes four separate counters to zero (see page 67 for a similar use of operator chaining). The for loop is then used to consider each individual base, with the compound `if` statement used to distinguish between the possibilities. The final `else` clause executes if all of the earlier conditions have failed. In this context, if we assume that the DNA data is legitimate, then if a base is not an A, C, or G, it must be a T.

The convenience of the `elif` syntax in this example is more significant. If we had been forced to nest multiple `if-else` constructs, this code must be formatted as

```python
numA = numC = numG = numT = 0
for base in dna:
    if base == 'A':
        numA += 1
    else:
        if base == 'C':
            numC += 1
        else:
            if base == 'G':
                numG += 1
            else:  # presumably a T
                numT += 1
```

The DNA example brings up another interesting lesson, beyond the syntactic issues. A careful reader may recall from Section 2.3.1 that the suite of methods supported by the `str` class includes a `count` method that calculates the number of occurrences of a specified substring. Therefore, we could accomplish our goal with the following approach.

```python
numA = dna.count('A')
numC = dna.count('C')
numG = dna.count('G')
numT = dna.count('T')
```

The question is whether one approach is clearly superior to the other. The code on this page is much simpler to develop and perhaps more intuitive to read.

Efficiency becomes a significant issue when working on a large strand of DNA (for example the human genome has roughly 3 billion bases). The fact that code appears simpler syntactically does not actually mean it is more efficient. In some respect, the work is shifted behind the scene into the `count` method. We might suspect the approach on this page to be slower, as the four separate calls to `count` probably cause four separate passes through the original data, as opposed to the single loop in our earlier approach.

Interestingly, if we run our own tests on large DNA strands, we find that the approach on this page is actually significantly faster than that of page 146 (roughly 5 times faster on our system). The primary reason for this discrepancy is that the implementation of the built-in `count` method is optimized to take advantage of the internal representation of a string. A conclusion we can draw from this example is that there is a strong argument to be made for using existing tools rather than reinventing them, especially if the tools are well suited and presumably optimized. Of course this is only a guideline; there are many ways to destroy the efficiency of a program by relying on tools that are not well suited for a task (such as using a screwdriver to drive nails).
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4.5 List Comprehension

In Section 4.1.1 we considered the goal of mutating a list of guests to convert all names to lowercase. A closely related task is that of creating a new list with lowercase versions while leaving the original unchanged. This is easily accomplished with the following code:

```python
auxiliary = []
for person in guests:
    auxiliary.append(person.lower())
```

This approach uses a general pattern in which we create a new empty list and then populate the new list by adding a corresponding entry for each item of the original list. While this implementation is straightforward, Python supports an even simpler syntax for such tasks known as list comprehension. This syntax resembles a list literal, but allows us to generate contents for a new list based upon entries of an existing list. As an example, the preceding code fragment can be replaced by the single command

```python
auxiliary = [ person.lower() for person in guests ]
```

This syntax provides a compact way of designating the four key components in the above example, using the form \( \text{result} = [ \text{expression for identifier in sequence} ] \). In evaluating this statement, Python iterates the for loop, appending the given expression to the new result during each pass. Notice that the expression `person.lower()` is allowed to depend upon the loop variable `person`.

There is a more general form of list comprehension with a condition that must be true in order for a corresponding entry to be appended to the result during each given iteration. That form is expressed using the syntax

```python
result = [ expression for identifier in sequence if condition]
```

This statement is evaluated similarly to the following nested control structures:

```python
result = []
for identifier in sequence:
    if condition:
        result.append(expression)
```

For example, suppose we want to scan a list of transactions and produce a supplemental list of all deposits from that original list. This can be done using the following list comprehension:

```python
deposits = [entry for entry in transactions if entry > 0]
```
4.6 Chapter Review

4.6.1 Key Points

For Loops

- A for loop is used to repeat a series of steps for each item of a sequence (e.g., a list, string, tuple).
- The general syntax of a for loop is the following:

  ```python
  for identifier in sequence:
    body
  ```

- For each element of an original sequence, the for loop identifier is assigned to that element and then the body is executed.
- The body of a loop can be an arbitrarily long block of code. The first line of the body establishes an indentation level. When the indentation returns to that of the word `for`, it is no longer considered to be part of the loop body.
- The body of the loop may contain an additional nested control structure.
- The list produced by the `range` function is a convenient sequence for iteration.
- An index-based loop is one that iterates over a list of indices of a list rather than over the original list, for example, `for i in range(len(guests))`.

Conditionals

- A conditional construct is used to specify commands that are only to be executed when a certain condition is met. The basic syntax of a conditional is the following:

  ```python
  if condition:
    body
  ```

  When the condition evaluates to `True` the body will be executed; otherwise the body is bypassed. The condition can be an arbitrarily complex boolean expression.
- An `if` statement can be followed by an `else` clause using the following syntax:

  ```python
  if condition:
    body1
  else:
    body2
  ```

  With this syntax, either the first or the second body will be executed (but not both).
- An `if` statement can be followed by one or more `elif` clauses to express subsequent conditions to be checked should the first one fail.

  ```python
  if condition1:
    body1
  elif condition2:
    body2
  ```

- An `if-elif` construct can optionally be followed by a final `else` clause that will be performed if all earlier conditions have failed.
List Comprehension

- Python offers a convenient syntax for creating a new list that has contents based upon the entries of an original list. The general form,

\[
\text{result} = [ \text{expression for identifier in sequence if condition} ]
\]

produces a result equivalent to that of

```python
result = []
for identifier in sequence:
    if condition:
        result.append(expression)
```

4.6.2 Glossary

- **body** A block of (indented) code used within the context of a control structure.
- **conditional statement** A control structure that specifies one or more blocks of code to be executed only if certain conditions are true.
- **control structure** A command that describes the order in which some other instructions are executed.
- **flow of control** The order in which a series of statements is executed.
- **for loop** A control structure used to iterate a block of code for each item of a sequence.
- **if statement** See conditional statement.
- **index-based loop** A loop that iterates over a range of integers representing indices of a list, rather than iterating directly over the elements of that list.
- **iteration** The process of repeating a step for each item in a sequence.
- **list comprehension** A syntax for creating a new list that is populated based upon the contents of an existing list, as in `deposits = [entry for entry in transactions if entry > 0]`.
- **loop variable** An identifier that is assigned to each element of the sequence during the execution of a for loop.
- **nesting** A technique in which one control structure is placed within the body of another.
- **short circuiting** A technique used by the computer in evaluating compound boolean expressions, whereby a partial evaluation suffices as soon as the outcome can be properly determined.

4.6.3 Exercises

**For loops**

**Practice 4.1:** Consider the following program:

```python
foods = ['eggs', 'broccoli', 'peas', 'salt', 'steak']
for ingredient in foods:
    print(ingredient[1])
```

Predict the output that results when this code is executed.
Practice 4.2: Given the string original create a new string dramatic that has two consecutive copies of each letter from the original string. For example, the dramatic version of 'argh' appears as 'aarrgghh'.

Practice 4.3: Given an original list of integers intList create a list strList that contains the associated string representations of those integers. For example, when starting with intList = [4004, 8080, 6502, 8086, 68000, 80486], the resulting list of strings should be ['4004', '8080', '6502', '8086', '68000', '80486'].

Practice 4.4: Write a program that draws an n-level staircase made of rectangles, such as the example for n = 4 shown here.

Exercise 4.5: Consider the following program:

```python
    t = 0
    for k in range(5):
        t += k
        print k, t
```

Predict the output that results when this code is executed.

Exercise 4.6: Write a short program that uses a for loop to animate a circle moving across a canvas.

Exercise 4.7: Rewrite the program for drawing a pyramid in Figure 4.8 so that it prompts the user for the number of levels and the overall height of the pyramid.

Exercise 4.8: Assume that word is a string, for example 'slice'. Write code to print out the following pattern for the given word:

```
s
sl
sli
slic
slice
```

Exercise 4.9: Write a program that prints an n-level staircase made of text, such as the example for n = 4 shown here.

```
*  
* *
* * *
* * * *
```
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Exercise 4.10: Write a program that draws an \( n \)-level staircase made of squares, such as the example for \( n = 4 \) shown here.

Exercise 4.11: Write a program that draws an \( n \)-level staircase as a single polygon, such as the example for \( n = 4 \) shown here.

Exercise 4.12: Assume that `people` is a list of names, each represented as a string using the format `'firstName lastName'`. Print out the names one per line, yet alphabetized by last name.

Exercise 4.13: Given a positive integer \( k \), write a program that calculates the factorial of \( k \), defined as

\[
k! = k \cdot (k-1) \cdot (k-2) \cdots 2 \cdot 1.
\]

Exercise 4.14: The mathematical constant \( e \), which serves as the base of the natural logarithm, is an irrational number with value approximately 2.718281828459. The precise value of this constant is equal to the following infinite series:

\[
e = \sum_{k=0}^{\infty} \frac{1}{k!}
\]

Although we cannot compute the entire infinite series, we get a good approximation of the value by computing the beginning of such a sequence. Write a program that approximates \( e \) by computing the sum of the first \( n \) terms, for some \( n \).

Exercise 4.15: The syntax `int('314')` converts the string of numerals to the corresponding (base ten) number. However, Python also allows you to interpret strings in a nonstandard base, specified as an optional parameter. For example the syntax `int('314', 5)` returns the decimal value 84. If viewed as a base five number, the string `314` represents \( 3 \times 5^2 + 1 \times 5^1 + 4 \times 5^0 \) and thus equivalent to the (base ten) value 84. Your goal is to convert such strings from scratch, without relying on the optional parameter form of Python’s `int()` conversion. Write a program that asks the user for the original string as well as the designated base (you may assume that the base is at most ten). Your program should compute and print the associated (base ten) value.

Exercise 4.16: In *A Word of Warning* on page 133, we consider the effect of a `for` loop body that mutates the structure of the list over which it is iterating. Run that code on
your computer and report the output that you see. Give a hypothesis, consistent with
your observations, as to what is happening behind the scene.

Exercise 4.17: Starting on page 146 of Section 4.4.2, we use conditionals to count the
number of occurrences of each base type in a DNA strand. Show how to accomplish
this task using a for loop, yet without any conditionals (nor use of `str.count`). Hint:
maintain a list of four counters, indexing that list using a technique similar to the
Case Study of Section 4.2.

Conditionals

Practice 4.18: Lists support a method to count the number of times that a specified value
appears in a list. Show that you can compute such a count without relying upon that
method. Specifically, assume that you have a list `collection` and a target `value`. You
are to compute the number of times that the value appears in the given collection.

Practice 4.19: Write a block of code that does the following. Assuming that `words` is a
list of strings, generate a new list `shortWords` that includes all of the original strings
with length 3 or less.

Practice 4.20: Carefully consider the following program:

```python
for x in range(20):
    if x % 9 == 0:
        print x, 'is divisible by 9'
    elif x % 3 == 0:
        print x, 'is divisible by 3'
```

Predict the output that results when this code is executed.

Practice 4.21: Carefully consider the following program:

```python
x = int(raw_input('Enter a value for x: '))
y = int(raw_input('Enter a value for y: '))
if x > 5:
    if y <= 3 and x > 8:
        print 'answer is A'
    else:
        print 'answer is B'
elif y > 6 or x < 2:
    print 'answer is C'
else:
    print 'answer is D'
```

(a) Predict the output if the user enters 4 and then 4.
(b) Predict the output if the user enters 9 and then 4.
(c) Predict the output if the user enters 1 and then 9.
(d) Predict the output if the user enters 6 and then 2.
Exercise 4.22: Carefully consider the following program:

```python
x = int(input('Enter a value for x: '))
y = int(input('Enter a value for y: '))
if y >= 7:
    print 'answer is A'
elif x < 4:
    if y > 4:
        print 'answer is B'
    else:
        print 'answer is C'
else:
    print 'answer is D'
```

(a) Predict the output if the user enters 4 and then 4.
(b) Predict the output if the user enters 2 and then 4.
(c) Predict the output if the user enters 1 and then 9.
(d) Predict the output if the user enters 2 and then 6.

Exercise 4.23: Consider the following program:

```python
foods = ['eggs', 'broccoli', 'peas', 'salt', 'steak']
for k in range(len(foods) - 1):
    if len(foods[k]) < len(foods[k+1]):
        print k
```

Predict the output that results when this code is executed.

Exercise 4.24: Carefully consider the following program:

```python
answer = 1
if greeting.count('a') == 1:
    if 'o' in greeting:
        if greeting.endswith('o '):
            answer = 2
        else:
            answer = 3
    else:
        answer = 4
elif len(greeting) < 6:
    answer = 4
print answer, greeting
```

For each of the following greeting values, predict the output that would result.
Exercise 4.25: Assume that we have a list of strings named `indonesian`. Give a sequence of commands that alters the list so as to replace each occurrence of the value 'java' with the value 'python' in its place.

Exercise 4.26: Write a code fragment that processes a list `items` and prints out all values that occur more than once on the list. Take care to only print out each such value once. For example, given the list

```python
items = ['apple', 'grapes', 'kiwi', 'kiwi', 'pear',
         'grapes', 'kiwi', 'strawberry']
```

your program should print

```python
grape
kiwi
```

(or kiwi, grape; either order will suffice).

Exercise 4.27: On page 141 we show how the short-circuit evaluation of the boolean operator `and` is equivalent to a nested conditional statement. The evaluation of the operator `or` also relies upon short-circuiting semantics. When the first condition is satisfied, there is no need to test the second condition; the compound condition is already satisfied. Give a nested conditional statement with semantics equivalent to

```python
if weather == 'rainy' or day == 'Monday':
    down = True
```

Exercise 4.28: Starting on page 144, we gave code to compute separate totals for the deposits and withdrawals on a list of transaction. That code used a single `for` loop with a nested `if-else` statement. Give an alternate implementation that achieves the same end results using a single `for` loop and a single `if` statement (without use of an `else` or `elif` clause).

Exercise 4.29: The precise value of the mathematical constant $\pi$ is equal to the following infinite series:

$$
\pi = 4 \cdot \left( \frac{1}{1} - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \cdots \right)
$$

Although we cannot compute the entire infinite series, we get an approximation to the value by computing the beginning of such a sequence. Write a program that approximates $\pi$ by computing the first $n$ terms, for some $n$. 

(a) 'adieu'  (b) 'aloha'  (c) 'bonjour'  (d) 'ciao'  (e) 'dia duit'  (f) 'goeie dag'
(h) 'hallo'  (i) 'hola'  (j) 'jambo'  (k) 'shalom'  (l) 'salaam'  (m) 'terve'
(c) 'bonjour'  (d) 'ciao'  (e) 'dia duit'  (f) 'goeie dag'
(g) 'guten dag'  (h) 'hallo'  (i) 'hola'  (j) 'jambo'  (k) 'shalom'  (l) 'salaam'
(m) 'terve'  (n) 'zdravo'
Exercise 4.30: In Exercise 4.15 we examined the conversion of a numeric string from a nonstandard base back to decimal. In that problem, we assumed that the original base was at most ten. For a base larger than ten, the issue is that we need a different symbol for each possible value from 0 to \( (\text{base} - 1) \). The standard convention in computer science is to begin using alphabet symbols, with \( \text{A} \) representing ten, \( \text{B} \) representing eleven, and so on. As an example, \( \text{int}('\text{FAB4}', 16) \) evaluates to \( 64180 = (15 \times 16^3) + (10 \times 16^2) + (11 \times 16^1) + (4 \times 16^0) \).

Update your earlier program to allow for the conversion for bases up to 36. When considering an alphabet character from the original string, you can determine whether it is a true digit using the \( \text{str.isdigit} \) method. When it is not a true digit, you can compute the appropriate value (such as 15 for \( \text{F} \)) by taking advantage of ASCII encoding with the following formula: \( \text{value} = 10 + \text{ord(symbol)} - \text{ord('A')} \).

List Comprehension

Practice 4.31: Redo Practice 4.2 taking advantage of list comprehension. Note that string comprehension can be used to iterate upon a string, but the result is always a list.

Practice 4.32: Redo Practice 4.3 using list comprehension.

Practice 4.33: Redo Practice 4.19 using list comprehension.

Exercise 4.34: Use list comprehension to create the list of values
[1, 2, 4, 8, 16, 32, 64, 128, 256, 512].

Exercise 4.35: Use list comprehension to generate the list of floating-point numbers
[1.5, 2.5, 3.5, 4.5, 5.5, 6.5, 7.5, 8.5, 9.5]

Exercise 4.36: The range function is only able to produce a list of integers. Given floating-point values \( \text{start} \), \( \text{stop} \), and \( \text{step} \), show how to create a list of floating-point values, starting at \( \text{start} \), taking steps of size \( \text{step} \), going up to but not including or passing \( \text{stop} \). For example with \( \text{start} = 3.1 \), \( \text{stop} = 4.6 \), and \( \text{step} = 0.3 \), the result should be the list [3.1, 3.4, 3.7, 4.0, 4.3].

Exercise 4.37: In the Case Study of Section 4.2 we used a for loop to create the \( \text{rnaList} \) base by base. Show how lines 5–9 could be replaced by a single list comprehension statement.

Exercise 4.38: Given a list \( \text{orig} \), possibly containing duplicate values, show how to use list comprehension to produce a new list \( \text{uniq} \) that has all values from the original but with duplicates omitted. Hint: look for indices at which the leftmost occurrence of a value occurs.

Projects

Exercise 4.39: Write a program that uses loops to generate an \( n \times n \) multiplication table for positive integer \( n \). As a model, here is a \( 4 \times 4 \) version of the desired format.

<table>
<thead>
<tr>
<th></th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>4</td>
</tr>
<tr>
<td>2</td>
<td>2</td>
<td>4</td>
<td>6</td>
<td>8</td>
</tr>
<tr>
<td>3</td>
<td>3</td>
<td>6</td>
<td>9</td>
<td>12</td>
</tr>
<tr>
<td>4</td>
<td>4</td>
<td>8</td>
<td>12</td>
<td>16</td>
</tr>
</tbody>
</table>
Hint: to properly line up the columns, you may rely upon the `rjust` method to right justify strings. For example, the expression `str(value).rjust(3)` produces a string of three characters with necessary leading spaces. For an $n \times n$ table, the maximum number of characters needed for one entry will be `len(str(n*n))`.

**Exercise 4.40:** Use the graphics library to create an image of a checkerboard with pieces placed in their initial configuration, as shown here.

![Checkerboard](image)

**Exercise 4.41:** Animate a ball moving across a canvas under the effect of gravity. You should maintain the position and velocity of the ball. During each iteration of the animation, the velocity should be used to update the position of the ball, and gravity should have a downward effect on the vertical component of the velocity.